

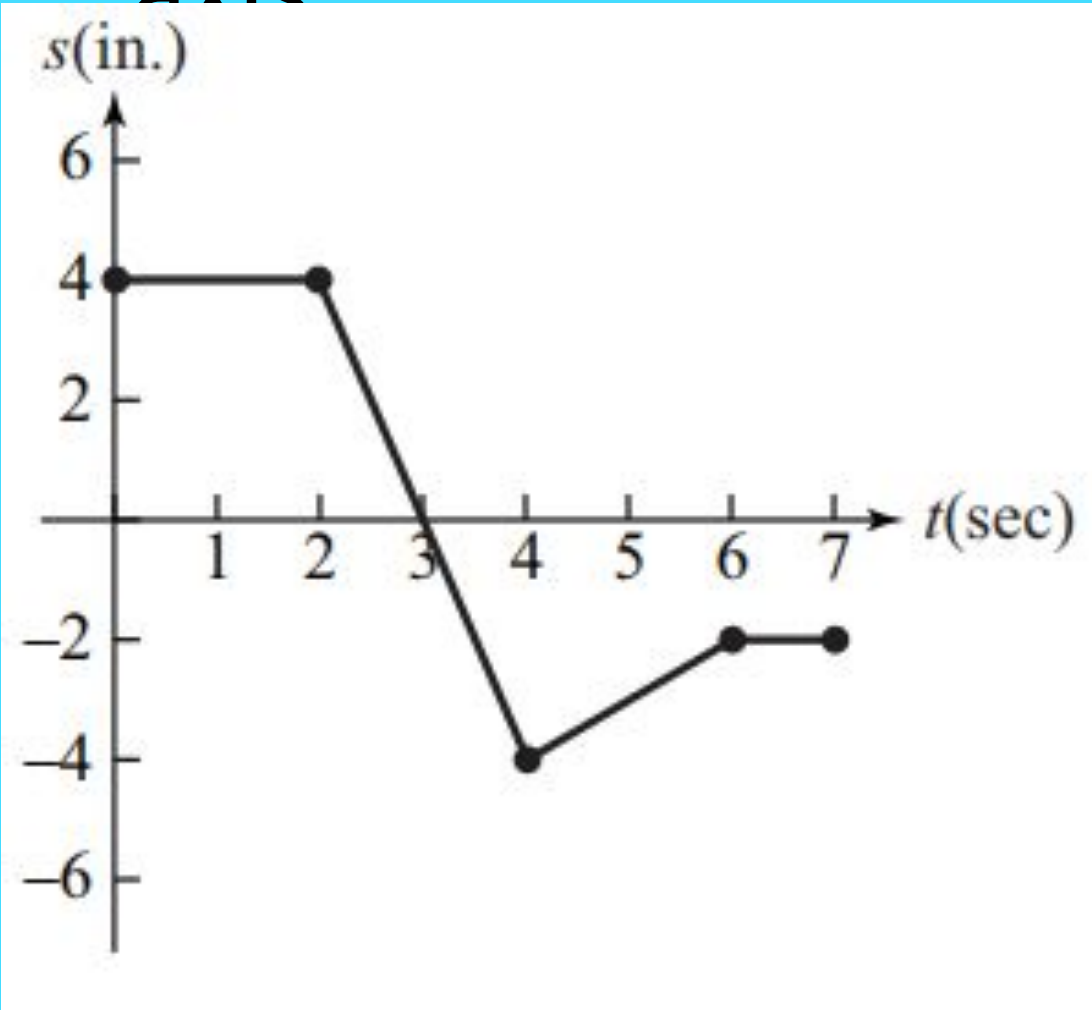
Find the derivative using the formal definition of derivative:

$$2/(X+3)$$

Particle Motion

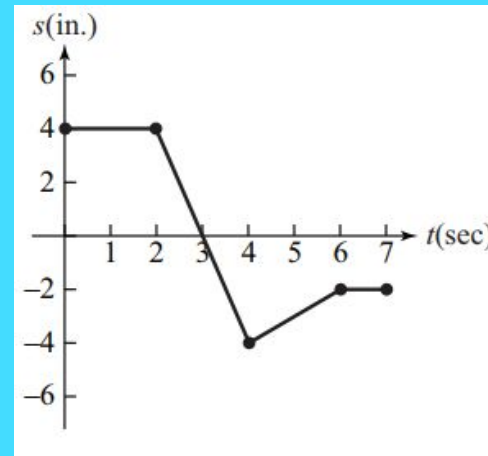
<https://www.youtube.com/watch?v=ZM8ECpBuQYE>

The graph shows the position $s(t)$ of a particle moving along a horizontal coordinate axis

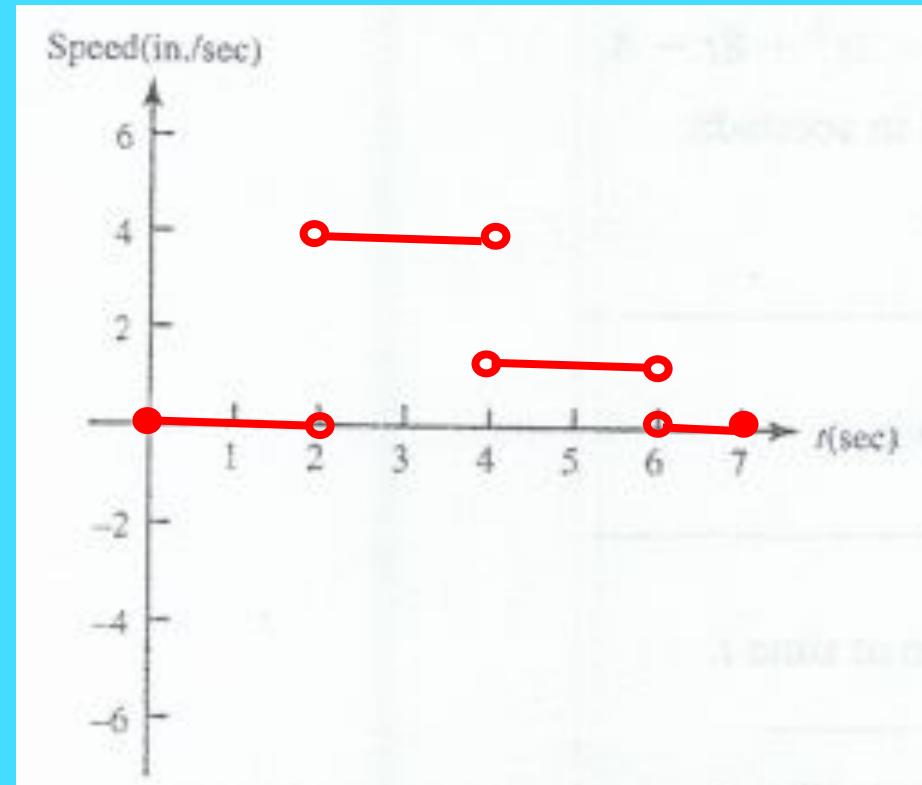
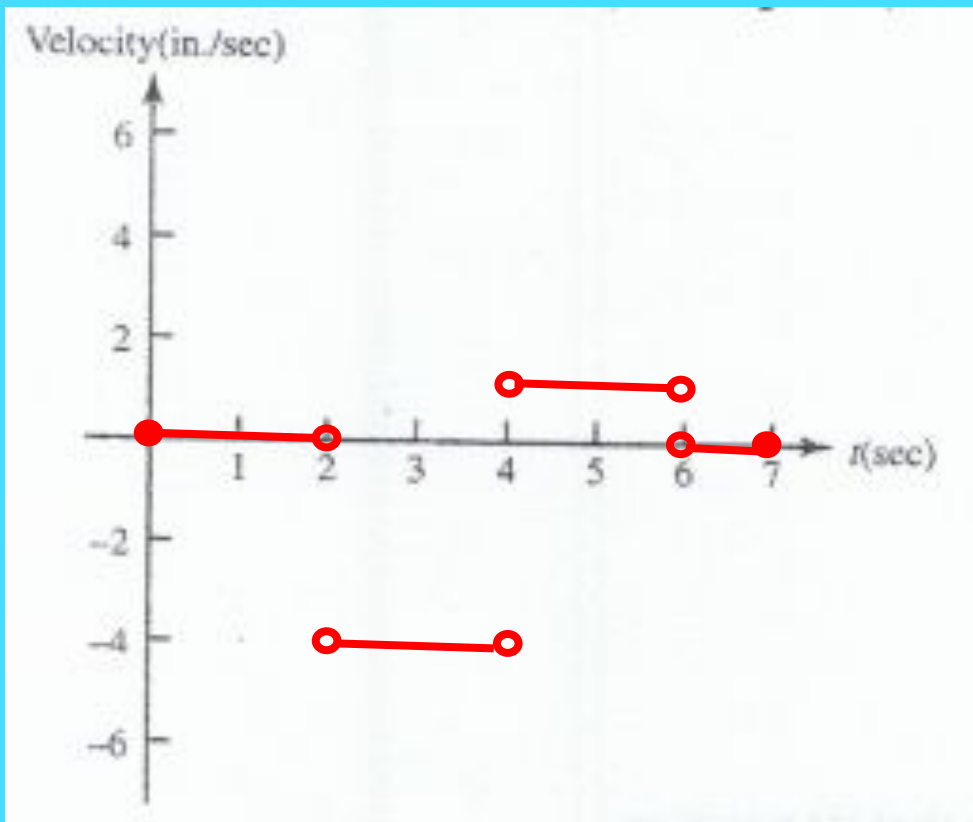


- a) When is the particle moving left? **(2, 4)**
- b) When is the particle moving right? **(4, 6)**
- c) When is the particle standing still? **$[0, 2] \cup [6, 7]$**

d. Graph the particle's velocity and speed (where defined)

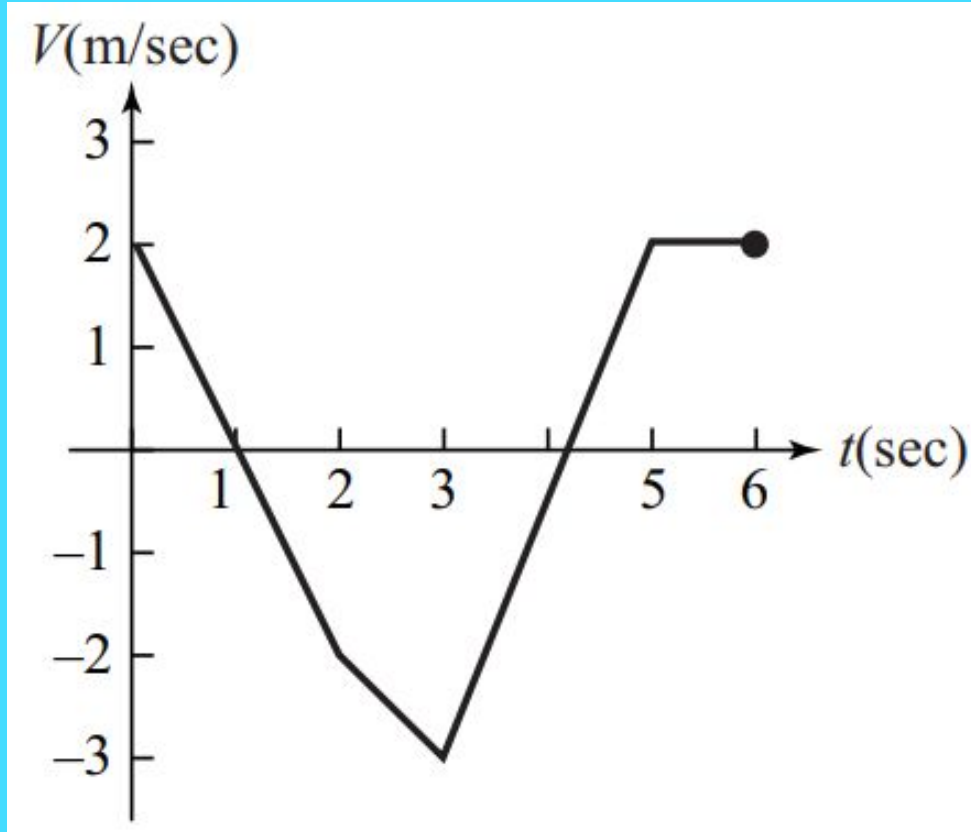


Keep in mind: $Velocity = \frac{\Delta position}{\Delta time}$ and $Speed = |Velocity|$



e. When is the particle moving fastest?

The graph shows the velocity $v=f(t)$ of a particle moving along a horizontal coordinate axis.

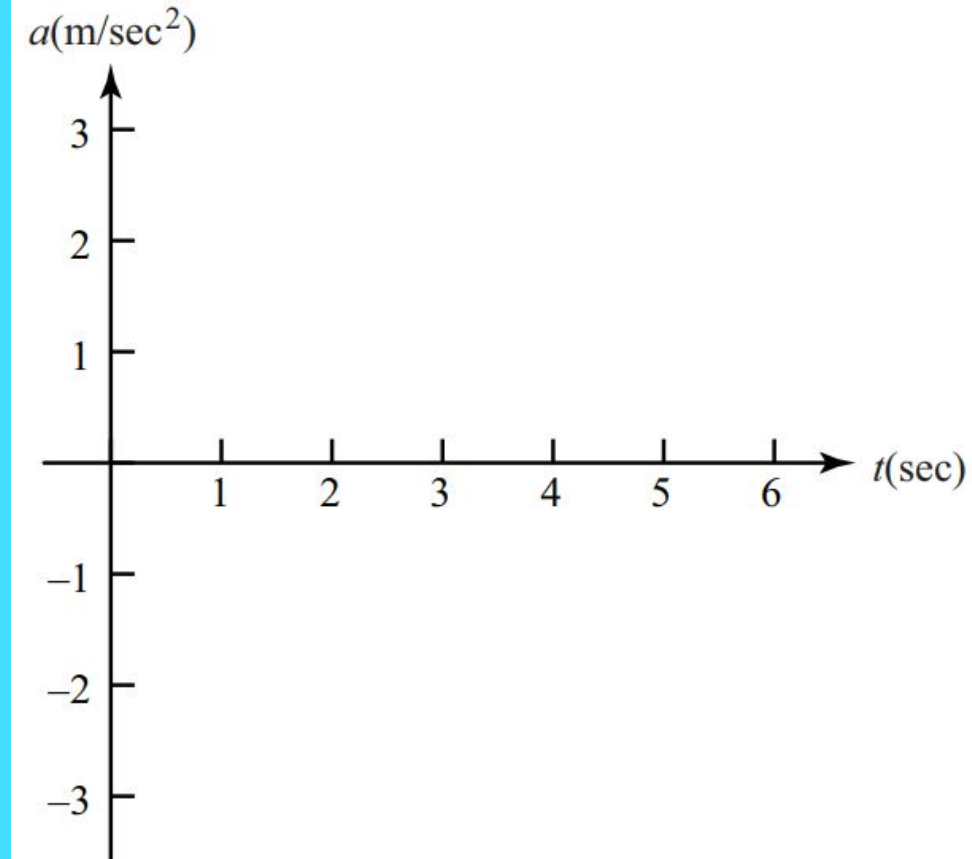
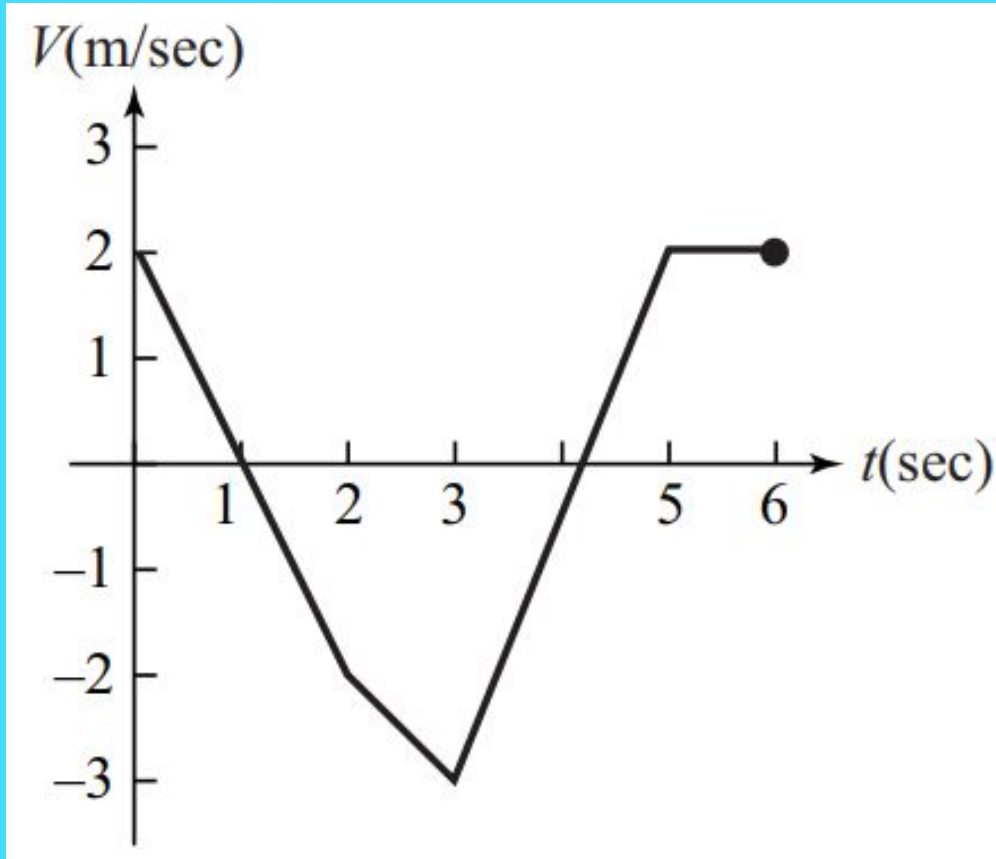


- a. When does the particle reverse direction? **$t=1, 4.25$ sec**
- b. When is the particle moving at a constant speed? **$(5, 6)$ sec**
- c. When is the particle moving at its greatest speed? **$t = 3$ sec**

d. Graph the acceleration (where defined)

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Keep in mind: $Acceleration = \frac{\Delta Velocity}{\Delta time}$



A particle moves along a vertical coordinate axis so that its position at any time $t \geq 0$ is given by the function $g(t) = \frac{1}{3}t^3 - 3t^2 + 8t - 4$.

- a. Find the displacement ($\Delta position$) during the first 6 seconds.

$$g(6) - g(0) = 8 - (-4) = 12$$

- b. Find the average velocity during the first 6 seconds.

$$Velocity = \frac{\Delta position}{\Delta time} = \frac{g(6) - g(0)}{6 - 0} = \frac{12cm}{6 sec} = 2 cm/s$$

c. Find expressions for the velocity and acceleration at time t. Hmm..

Velocity = $\frac{\Delta \text{position}}{\Delta \text{time}}$ AKA SLOPE of the position function

And

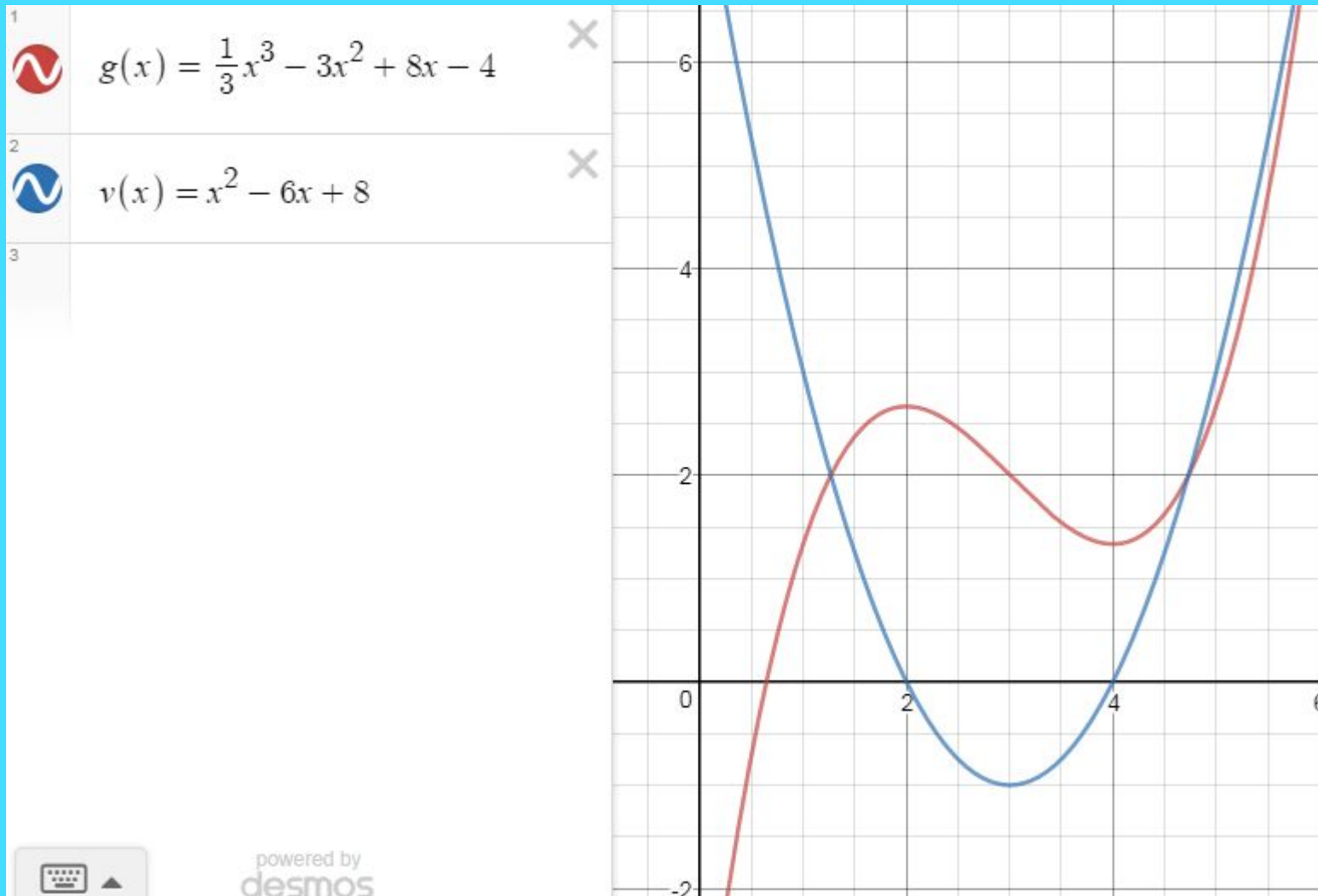
Acceleration = $\frac{\Delta \text{Velocity}}{\Delta \text{time}}$ AKA SLOPE of the velocity function

So if the position at time t is modeled by $g(t) = \frac{1}{3}t^3 - 3t^2 + 8t - 4$

Velocity at time t can be modeled by: $v(t) = t^2 - 6t + 8$

Acceleration at time t can be modeled by: $a(t) = 2t - 6$

d. For what values of t is the particle moving downward?



Look at the graph of either the position function or the velocity function!

(2, 4) on the red graph (position) shows a negative slope

(2, 4) on the blue graph shows a negative velocity (movement in the negative direction)

e. Find the total distance traveled from 0 to 6 seconds.

$$g(0) = \frac{1}{3}(0)^3 - 3(0)^2 + 8(0) - 4 = -4$$

$$g(2) = \frac{1}{3}(2)^3 - 3(2)^2 + 8(2) - 4 = \frac{8}{3}$$

$$g(4) = \frac{1}{3}(4)^3 - 3(4)^2 + 8(4) - 4 = \frac{4}{3}$$

$$g(6) = \frac{1}{3}(6)^3 - 3(6)^2 + 8(6) - 4 = 8$$